

Feige-Fiat-Shamir ZKP Scheme Revisited

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Abstract

In networks and entity groupings that have sensitive resources, user identification is a crucial requirement for secure access, communication and transactions involving those resources. However, there are networks and entity groupings that require entity authentication while preserving the privacy of the entity being authenticated. There are several zero-knowledge protocols (ZKP) including the Feige-Fiat-Shamir that authenticate an entity anonymously. We present a revised Feige-Fiat-Shamir ZKP scheme for the Airborne Networks (ANs) that reduces the ping-pong effect in the scheme and speeds up the growth of the Verifier trust of the Prover, thus making the authentication process faster and more efficient.

Key Words: Mission critical, time, authenticity, anonymity, zero knowledge, authentication.

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1. INTRODUCTION

In agile networks and other entity groupings that are mission driven, time sensitive, ad-hoc and self-organizing like in the Airborne Networks (ANs), authenticity, anonymity and accountability are essential and crucial and probably more so than in other similar networks that are less mission critical and time sensitive. In these kinds of networks, standard cryptographic authentication protocols like PKI cannot work effectively.

An Airborne Network is a self-forming, self-organizing, and self-generating, mission-critical and time sensitive network of airborne entities as nodes joining and leaving the network as they enter and exit specific regions. The network consists of dedicated tactical links, wideband air-to-air links, and ad-hoc networks constructed by the Joint Tactical Radio System (JTRS) networking services (Wikipedia [2009]). In addition, the JTRS is a software-defined radio that normally works with many existing military and civilian radios with the help of an integrated encryption and Wideband Networking Software that also provides system performance analysis and fault diagnostics automatically, reducing the demand for human intervention and network maintenance (Austin Mohr, [2007]).

There several efficient proofs including classical formulations of NP, interactive proof systems, computationally-sound proof systems, and probabilistic checkable proofs that can be good candidates for the ANs. However, the most suitable are proofs in the interactive proof systems. In particular, the zero-knowledge proof system (ZKP defined as Oded Goldreich [1993]: *For a language L a zero-knowledge proof system is a pair (P, V) of interactive machines, so that V is probabilistic polynomial-time, satisfying*

- *Completeness: For every $x \in L$ the verifier V always accepts after interacting with the prover P on common input x .*

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- Soundness: For every x not in L and every potential prover P^* , the verifier V rejects with probability at least $1/2$ after interacting with P^* on common input x .

The *Prover* P is a machine that is seeking authentication that must be done by the Verifier V upon presentation of evidence by the *Prover* to the Verifier that does not give away the identity of the *Prover*. Based on the evidence provided by the *Prover*, the verifier may get satisfied and authenticate the *Prover* without knowing the identity of the *Prover*. Unlike the Public Key Infrastructure (PKI), a framework for creating a secure method for exchanging information based on public key cryptography. The key role for the PKI is the certificate authority (CA), which issues digital certificates that authenticate the identity of entities over a public communication system as the Internet. ZKP does not involve this CA acting as a third party.

In ZKP, the *Prover* presents to the *Verifier* a publically generated and known part of the token. Upon receiving the public part of the *Prover's* token, the Verifier then may require the *Prover* to produce a *response*, to a Verifier's randomly generated *challenge* based on the *Prover's* public part of the token. On receiving the *Prover's* response, the *Verifier* then validates the response using no more than the publicly known information. Two possible outcomes are either "yes" or "no". If a "yes" answer is produced, the authentication process is successfully over and the token is now *spent*, meaning, it has served its purpose and it is done. Any other authentication needed by this entity requires a new token to be generated. If the outcome is a "no" a new round of authentication may be required. This may go on for a number of back and forth ping-point exchanges until success. A successful ZKP authentication leads to the *Prover* remaining anonymous to the verifier.

Several scholars (Park Choonsik [1992], Dev Anshul and Suman Ray [2005], M. J. Fisher [2005], Hannu A. Aronsson [2000]) have written about the problems of ZKP protocols including their inefficiency in exchanging tokens during the *challenge-response* sessions. Such problems tend to get worse as the network sizes grow.

In this paper we propose a new approach to the Feige-Fiat-Shamir ZKP scheme that aims to reduce the number of *challenge-response* ping-pong exchanges and thus create a speed-up in the building of trust and increasing the effectiveness of the scheme.

The rest of the paper is organized as follows. We will introduce the Feige-Fiat-Shamir ZKP Scheme in Section 2. Then we will explain the new improvements to the Feige-Fiat-Shamir Protocol scheme in Section 3. Security and trust analysis will be given in Section 4. Problems with Parallel Execution of Zero-Knowledge Proofs are discussed in Section 5. Finally we conclude and discuss possible extension in Section 6. References are in Section 7.

2. RELATED WORK

Several interesting zero knowledge proofs are of note here starting with Hannu Aronsson,s (Wikipedia [2009]) work which explains zero knowledge proofs starting with the basics including a summary of all the major zero knowledge studies. Li Lu et al [2006] discuss zero knowledge authentication in P2P systems. However, they use a modified ZKPI scheme that uses a key exchange but with no third party. Austin Mohr [2007] gives an in depth survey of zero knowledge proofs ranging from Graph Isomorphism, Graph 3-colorability, All Languages in NP and Fiat-Shamir protocol. None of these works attempts to extend the speed of authentication as ours attempts to do.

3. FEIGE-FIAT-SHAMIR PROTOCOL

The Feige-Fiat-Shamir Identification Scheme is a classical, practical and widely used modular arithmetic ZKP scheme developed by Uriel Feige, Amos Fiat and Adi Shamir in 1988. Following the principle of all zero-knowledge proofs, the Feige-Fiat-Shamir Identification Scheme involves two entities, the *Prover*, and the *Verifier*. The *Prover* possesses a secret token and is seeking authentication and must prove to another entity, the *Verifier*, who must authenticate the *Prover* based upon the secret token the *Prover* has, through a series of challenges without getting to know the *Prover's* secret token.

Procedure

The Feige-Fiat-Shamir process involves the *Prover* choosing two large Blum prime integers p and q where each is of the type $4g+3$ and $\gcd(g, 3) = 1$. Also the *Prover* chooses two security integers k and t . Then computing the product $n = pq$. The protocol then uses this n in the modular arithmetic that follows. The congruence relation

Two integers a and b are said to be *congruent modulo*, if their difference $a - b$ is an integer multiple of n . That is both numbers have the same remainder when divided by n . This is then expressed as:

$$a \equiv b \pmod{n}.$$

A good example are integers $a = 38$ and $b = 14$. Then $38 \equiv 14 \pmod{12}$ shows that (a, b) form a congruence class.

Using this n , choose or create secret vector $s = \{s_1, \dots, s_k\}$ with $\gcd(s_i, n) = 1$, and $c = \{c_{i=1, k} | c_i \in (0, 1)\}$. n is then made public. Now compute the vector $v = \{v_1, v_2, \dots, v_k | v_i \equiv s_i^2 \pmod{n}\}$ where \equiv is a congruency relation between v_i and s_i^2 , meaning that v_i and s_i^2 have the same remainder upon division by n .

The vector v then is sent to the *Verifier*. The difficulty the *Verifier* may encounter in recovering the vector s as it involves the computation of the modular square root without knowing the modulus' factorization. The Feige-Fiat-Shamir procedure goes as follows [7].

1. *Prover* chooses a random integer r , a random sign $b \in \{-1, 1\}$ and computes $x \equiv (-1)^{c_{i=1, k}} \cdot r^2 \pmod{n}$. *Prover* sends this number to *Verifier*.
2. *Verifier* chooses numbers a_1, \dots, a_k where a_i equals 0 or 1. *Verifier* sends these numbers to *Prover*.
3. *Prover* computes $y \equiv r s_1^{a_1} s_2^{a_2} \dots s_k^{a_k} \pmod{n}$. *Prover* sends this number to *Verifier*.
4. *Verifier* checks that $y^2 \equiv \pm x v_1^{a_1} v_2^{a_2} \dots v_k^{a_k} \pmod{n}$.

This procedure is repeated with different r and a_i values until *Verifier* is satisfied that *Prover* does indeed possess the modular square roots (s_i) of his v_i numbers.

4. THE REVISED FEIGE-FIAT-SHAMIR PROTOCOL

The Ping-Pong Problem

While the Feige-Fiat-Shamir Identification Scheme is the most celebrated, classical, practical and widely used modular arithmetic ZKP scheme, it suffers from the *ping-pong problem*. The Ping Pong problem in the ZKP solutions is caused by repeated, sometimes uncontrolled, challenge-response exchanges between the *Verifier* and the *Prover*, as the *Verifier* tries to get as much information as possible from the *Prover* in order to complete the authentication process in the shortest time possible but in the most sure way and as the *Prover* tries to provide the needed information for the authentication process without revealing the *Prover's* identity. The ping-pong problem is a resource guzzler. Given that the AN environment is time critical, the authentication process needs to be comprehensive, precise and take a short time. But in the Feige-Fiat-Shamir this cannot be accomplished because, there is no sure way of making the process short. In some cases, the authentication process may be short but not always. We propose a procedure that speeds up this process and it builds the trust quickly. The scheme still involves two entities, the *Prover*, who possesses a secret token and is seeking authentication and must prove to another entity, the *Verifier*, who must authenticate the *Prover* based upon the secret token the *Prover* has, through a limited series of challenges without getting to know the *Prover's* secret token.

Procedure

The revised Feige-Fiat-Shamir protocol still involves the *Prover* choosing two large Blum prime integers p and q where each is of the type $4g+3$ and $\gcd(g, 3) = 1$. Also the *Prover* chooses two security integers k and t . The *Prover* then computes $n = pq$. Using this n , the *Prover* then chooses or creates a secret vector $s = \{s_1, \dots, s_k\}$ with $\gcd(s_i, n) = 1$. n is then made public. Further the *Prover* still computes the vector $v = \{v_1, v_2, \dots, v_k | v_i \equiv s_i^2 \pmod{n}\}$. The vector v is then sent to the *Verifier*. Like in the original Feige-Fiat-Shamir protocol, the Holy Grail of the protocol is the difficulty the

Verifier encounters in recovering the vector s as this involves the computation of the modular square root without knowing the modulus' factorization. The revised Feige-Fiat-Shamir protocol then goes as follows.

1. *Prover* chooses a random integer r , a random sign b in set $\{-1, 1\}$ and computes $x \equiv b \cdot r^2 \pmod{n}$. *Prover* sends this number to *Verifier*.
2. Each time the *Verifier* chooses a challenge, there are 2^k possible ways to choose the vector $a = \{a_1, \dots, a_k\}$ where a_i equals 0 or 1. These choices are represented by the 0-1 matrix $M = \{(a_{ij}) = (0,1) \mid (i,j) = 1, k\}$. From these rows of M , the *Verifier* randomly selects a number of rows forming a sub-matrix $D = \{(a_{ij}) = (0, 1) \mid i=1, k, j=1, f.\}$ of M to concurrently send to the *Prover* as the challenge.
3. Instead of the *Prover* computing only one number y , the *Prover* uses the received matrix D to compute a vector $y = \{y_1, y_2, \dots, y_f \mid y_i \equiv r \pi s_i^{a_{ij}} \pmod{n}, i=1..k \text{ and } j=1, f.\}$. The *Prover* then sends this vector y to the *Verifier*.
4. *Verifier* checks that each of the vector components of y satisfies $y_i^2 \equiv \pm x \pi v_i^{a_{ij}} \pmod{n}, i=1..k$ and $j=1, f\}$.

This procedure may be repeated with different r and different sub-matrices $D = \{(a_{ij} \mid i=1, k, j=1, f.)\}$ of M until the *Verifier* is satisfied that the *Prover* does indeed possess the modular square roots (s_i) of his v_i numbers.

An Example:

1. Suppose either the *Prover* or a trusted center T selects the primes $p = 139$, $q = 347$, and publishes $n = pq = 48233$.
2. The *Prover* chooses integers $k = 3$ and $t = 1$ as the needed security parameters.
Then the *Prover* does the following:
 - o Selects 3 random integers $s_1=87$, $s_2= 21649$, $s_3 = 523$, and 3 bits $b_1 = 1$, $b_2 = 0$, $b_3 = 1$.
 - o Computes $v_1 = 7569$, $v_2 = 10310$, and $v_3 = 32364$.
 - o The *Prover's* public key then is $(7569, 10310, 32364, 48233)$ and the *Prover's* private key is $(87, 21649, 523)$.
3. The *Prover* chooses integers $r = 3209$, $b = 1$, and computes $x = 24052$, and sends this to *Verifier*.
4. Since k was chosen as 3, the *Verifier* has the following possible matrix $M = \{000, 001, 010, 011, 100, 101, 110, 111\}$ of choices of challenges.
5. Suppose the *Verifier* chooses a sub-matrix $D = \{010, 011, 111\}$ and sends it to the *Prover*.
6. The *Prover* must compute a vector $y = \{y_1, y_2, y_3\} = \{16121, 5788, 36823\}$
7. The *Verifier* computes $(y_1^2, y_2^2, y_3^2) = (259886641, 33500944, 1355933329)$. Also computes $((24052*[10310], 24052*[10310*32364], 24052*[7569*10310*32364])$
8. To accept the *Prover's* identity the following pairs of numbers must be in the same congruency classes mod 48233:
 - a. $(259886641 \text{ and } 24052*10310)$
 - b. $(3350094 \text{ and } 24052*10310*32364)$
 - c. $(1355933329 \text{ and } 24052*7569*10310*32364)$

5. SECURITY AND TRUST ANALYSIS

Using the scheme we have outlined above one achieves tremendous savings first in time speed up and rapid build up of the trust and also in the security which is not compromised. Based on the Feige-Fiat-Shamir protocol on which this scheme is built, the *Prover* does not give any useful information to the *Verifier* during the whole process. If there is any interception of the communication, the interceptor can learn no more information than what the *Prover* gives out. The knowledge of the *Prover's* secret cannot leak because it is not communicated to the *Verifier*. The new scheme adds nothing that would change this fact. Therefore the security of the scheme is assured.

The major contribution of this scheme is a quick build up of the *Verifier* trust and confidence for the *Prover*. We can calculate this trust build up as follows. Suppose the security integers chosen by the *Prover* are k and l . This means that the *Verifier* has $k!$ ways of choosing a 0-1 vector of length k . This is what we referred to in the protocol as matrix M . Suppose further that the *Verifier* decided to send several of these vectors at a go. The *Verifier* can decide to send to the *Prover* a sub-matrix D of M consisting of these choices, the *Prover* then sends back the vector $y = \{y_1, y_2 \dots y_f\}$. At each parallel burst resulting in matrix D of f rows, with k bits each, which the *Prover* returns correct, the *Verifier*'s trust/confidentiality grows as $\{1 - ((1/2)^f)^k\}$. So for t bursts of parallelism, the contribution to trust increases by $\{1 - (((1/2)^f)^k)^t\}$. This is a good speed up which makes the authentication process take less time.

6. PROBLEMS WITH PARALLEL EXECUTION OF ZERO-KNOWLEDGE PROOFS

Parallel executions of zero-knowledge in Feige-Fiat-Shamir protocol have been proposed and they are certainly attractive and they reduce the number of ping pong messages between *Prover* and *Verifier* to only $1/2$. However, it has also been proven that they may not be fully zero knowledge (Joe Kilian, Eriz Petrank and Ransom Richardson [2001], M. Konidala Divyan [2003]). However, there have also been concurrent zero knowledge techniques that preserve zero knowledge (Li Lu, Jinsong Han, Yunhao Liu, Lei hu, Jinpeng Huai Lionel Ni and Jian Ma [2006]). Our approach consists of bursts of parallelism while maintaining serial execution of the Feige-Fiat-Shamir, hence maintaining zero knowledge. Note that the difference between the serial and full parallel versions of the protocol is that in the latter, the *Verifier* gets to know all of the x_i 's before choosing the b_i 's. This does not happen in our approach. The *Verifier* chooses matrix D with no knowledge of all the x_i 's. We generate bursts of parallelism consisting of matrices D with no more than $f < k$. The matrices D can be calculated several times depending on the number of bursts of parallelism that can occur during an entity authentication. This number, however, cannot be more than t .

7. SIMULATION AND RESULTS

The full simulation to support this paper was planned to be carried out in two phases as follows:

- (1) In phase one we planned to generate and test the C code developed by Daniele Raffo [2002] at LIX, Ecole Polytechnique, France. This code was modified and run in two modes, the single processor mode and the multi-processor distributed environment. In the single processor mode, we made several runs of the modified code and in the distributed environment, we developed the handshake protocols for the exchange of information between the *Prover* and the *Verifier* processors in a client-server model.
- (2) In phase two, we plan to develop new C++ code for the revised Feige-Fiat-Shamir zero-knowledge protocol discussed in this paper. Next we will develop the handshake protocol for the new FFS. We will then develop the test databed. With the test bed we will do:
 - Distributed testing
 - Speed up protocol development
 - Testing using UAVs as needed and where possible.
 - Analysis of results

In phase one, we have ran the modified C code on a trial basis and Figure 3 shows the outputs of those runs for $T = 10$ and $K = 10$. The results in Figure 3 show the full range of outputs which included modulus n , both the computed public and private keys after each of the ten iterations, the challenge from the *Verifier*, the response from the *Prover*, the verification by the *Verifier* and the acceptance by the *Verifier*. Since the growth of the output data was astronomical, we decided not to continue with this kind of experimentation.

Figure 3 (below): Row output from the Modified C Code.

Publishing modulus:

```
17976929205606008571648315122074122220102965845447940859554850840430813475670227100983
50184399271343467327287010688126007525809674107012108387332202665407984759216729068028
82425893135819150850301344123141412498892491036325633388257822297629447413753876149348
543391157235192405410661330286251829642799867610529
```

Computing keys

Public key:

1325625557264271676024090692164773830765799713043117227528632926510949761102233108196
 70413057761792102446546320619998748411283056671496121877666821840103407959409519981908
 78611212440363356690228646676543478072735080886180579618611185316085836814910668700772
 178596560234925155243849909292527807550786877325598
 13630403996302298141597863520177809111947610288203571012081079651181218746884402523762
 20058072988193501083406566024325204606396729189849440291576507536446421239343452602583
 27761305898784680879130656098014757732014784847792044698460542621432342880193923989712
 919728007258096777490561336107137968867636283902048
 91524625548709623598418881393288380896783392652190265032824063636517630562184208441303
 7521431510401386114916604373729836897761673750514279370537015098821581567292055666783
 81788937355133260675570024672415472418635228778601597110306827080098068875239606914108
 69205169388675058531657737809022786877712859474204
 10852062878736044524314651638729447161297468389151454417802470349123506768218846068339
 11090569231214982176846381546963135532020974113012816754717906695444111705386327157287
 40220422386313382819937149948836131324128486088451484832130008634654758421957003736829
 421218280063884645322699022818175881111555620622870
 17394490629576510437597664352437135834914159329103498549131612574992273407611080476852
 40070190865568825483418296403012259228105299377238410890844699832836567519277521855183
 48206923304195027873271778735162035470605419467891818866408142508253820293651028149625
 047926425499421469277319174658471647502125928532510
 11192529250098233222560673627420816678837136040240815033214924870733065091217240716506
 00836011004285414163587152789603446254793658690879244688162843792920636924413875355941
 97753738090593907545516297554607535208626264617259399720566423147202578117585748144902
 387479301022375529173683061506082526232204371185397
 92822503344974732701231405311799192202978414254399253894641868595667210911014724422953
 21878856186443399071038058578165851453560517385105019683059129891552161417771424498696
 3187242552904497948391365064318696072866608208562762985912544545726265027644174116532
 42477282844391921437713347501056915587463871075507
 76931730949259744103100800308564752542843555547705107776671639827301410839566750531691
 52468498678481836164149403102781116890658043996620446432123302772274904580602048853758
 37350747078469588651376415860835222218173266622068879398827422477356863499098915128259
 35677309360153288153649217180267901410989728935960
 17109148207572442309009686117360022096200899570941288416101391003975383768152279674908
 89675787141095611460464349046975878733196601462758601938116944554369826743793313913529
 01132735936739840420010040771266522528130151911240828912866528466536723715546441664009
 93757337504595597246022460444794694869785121025584
 54516656676446923506005618677267170596564581804575722672296464343354322039612834722878
 4259841133878308587422191553209646448919081033414438291603980280329575946055220270198
 06460974471618666362227087465044490552882058611657174179550983513384320904827797158689
 53774778799231113999655111292238975808537523924524

Private key:

15090651724267505309971848528182817639762883484063720504346210872054567712535887261764
 89265163983867716116255306927666719477521261840399065391330144079770376099761751215442
 82687798173836378706311506665888654639606166137472813102465213217334575444498611594443
 601103317781106636911139835814853151103961218939133
 12194695208480035384868695688957628159499601416962764459987609475311425548571694122189
 31365647753497958459354506658130861780634363463660655122330567364616594193237206603357
 68596576290810297389822595126022597737722063931686360491382793095922723028253192119896
 767408290847272964868484796815942952909768991176838
 15619200158546778457984510695972153067936715835277119391422623661283202164783846408379
 16336747828474279324350783269220108689219839878918813072043990466030737399672906376065
 03164678179518816642292522021767149970747002768545690951029354992973819220887304803952
 261707336114172928800409692135487768743212955435166

26261632180250039527648080517051390806459256463789623024410865947137884302656392540949
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 96353024807251173969339243496512031149359004192311877793629404155686210185425658165813
 02156111293234815117318936031296070289412465381448
 11152088734908610854001180587543354757635655365251931096578533904100419123149331085750
 16168915650232714365275784852247165274114356038483966025493126835360586631296179514402
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 540911317705978858597970076821734929582807389245610
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 12688048269240852856198759049205712364821231577104130321619098154241708195085827674163
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 69276458231405997136394987211967912986614047232992950838418542896590241758204040896430
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 28842437646076567506154422619070607560474175277643193330157138602685665678771521266105
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 66457423698969402991813166828200639023406606582801940676118130300251139098434855327309
 39535950599290310521513915746803185223170704593613025662567332562758396647335087599282
 18076896894025010867690566333882786485789593560811990148860902775540028313300222314199
 00749205277003448738458216286098718567909392354774

Witness

10089446400984104971521694311524167511941460331746945169456017920581446401327809173927
 45476319978048224998062463459693576765658363118819438361461271262703463212570763281231
 30112367302118118424573183118805902123632347050642989532098727171794810063859213630048
 849323533068447522197721951395940291447402660685747

Challenge : 1001001110

Response

78101732753568861159059663171867874182426270668817775078298424873689447719240465683969
 32489913456343487198548542240535084373605548162504832332491553866493744768880279715678
 78130092780222602026065928471647189815816541780156982466070464313262562931634068969091
 9360148727479600709380214702228401577776338882897

Verification:

10089446400984104971521694311524167511941460331746945169456017920581446401327809173927
 45476319978048224998062463459693576765658363118819438361461271262703463212570763281231
 30112367302118118424573183118805902123632347050642989532098727171794810063859213630048
 849323533068447522197721951395940291447402660685747

Authentication successful!

Next we restructured and expanded this code to convert it into C++ so that we could run both the Prover and the Verifier codes as threads. Several runs were made with varying sizes of K, T and time tamps. Figure 4 shows selected outputs of these runs except the varying time stamps for each change in T and K. We are showing a selected number of runs of varying sizes of Ts and Ks using a single core thread environment:

Figure 4 (below): Selected Runs with Varying Sizes of Ts and Ks Using Threads

T = 10, 100, 500, 1000, 2000, 5000.

K = 10, 20, 50, 70, 100, 500

Sample Runs:

1. $T=5$ and $K = 4$

Feige-Fiat-Shamir ZKP implementation

Iteration 0: 06.12.2009 22:24:27

Authentication successful.

Iteration 0 finished at: 06.12.2009 22:24:27

Iteration 1: 06.12.2009 22:24:27

Authentication successful.

Iteration 1 finished at: 06.12.2009 22:24:28

Iteration 2: 06.12.2009 22:24:28

Authentication successful.

Iteration 2 finished at: 06.12.2009 22:24:28

Iteration 3: 06.12.2009 22:24:28

Authentication successful.

Iteration 3 finished at: 06.12.2009 22:24:28

2. $T=10$ & $K = 8$

Feige-Fiat-Shamir ZKP implementation

Iteration 0: 06.12.2009 23:31:07

Authentication successful.

Iteration 0 finished at: 06.12.2009 23:31:07

Iteration 1: 06.12.2009 23:31:07

Authentication successful.

Iteration 1 finished at: 06.12.2009 23:31:07

Iteration 2: 06.12.2009 23:31:07

Authentication successful.

Iteration 2 finished at: 06.12.2009 23:31:07

Iteration 3: 06.12.2009 23:31:07

Authentication successful.

Iteration 3 finished at: 06.12.2009 23:31:07

Iteration 4: 06.12.2009 23:31:07

Authentication successful.

Iteration 4 finished at: 06.12.2009 23:31:07

Iteration 5: 06.12.2009 23:31:07

Authentication successful.

Iteration 5 finished at: 06.12.2009 23:31:07

Iteration 6: 06.12.2009 23:31:07

Authentication successful.

Iteration 6 finished at: 06.12.2009 23:31:07

Iteration 7: 06.12.2009 23:31:07

Authentication successful.

Iteration 7 finished at: 06.12.2009 23:31:07

K	Seconds
10	1
50	3
100	3
500	10
1000	34
2000	119
3000	296
4000	509
5000	807

Table 1: Changing values of K, T =20 and the time stamps.

To learn more of these changing timestamps, we extended this algorithm so that it can work in the multi thread and truly distributed environment of a client-server model by developing communication protocols and handshake necessary in a networked environment. Under this environment, the Verifier runs as the server and the Prover as the client. In this Client-Server model, we tested the algorithm on differing sizes of both K and T. As we did this, the time stamp was taken at the start and end of each exchange between the client and the server until the Verifier accepted the Prover.

In Table 1 and corresponding Figure 5 we show results of runs in this distributed client-server environment with varying sizes of K.

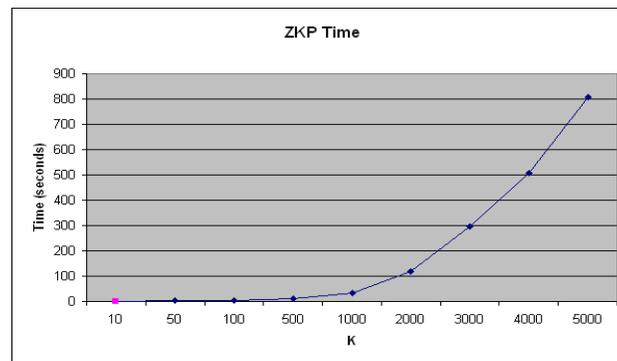


Figure 5: Growth of Computation Time Against the Size of the Primes K.

From Figure 5 above, there is compelling evidence that the larger the size of the integer strings, the longer it takes for the authentication of the entity.

9. ZKP COMPARED TO PKI

We have not compared ZPK with suitable PKI yet but this will be our next step.

10. FUTURE WORKS

As we pointed out earlier, this work has so far dealt with the original Feige-Fiat-Shamir. The simulation of the Feige-Fiat-Shamir discussed in full is to be tackled in the planned phase II of this work. This will be the starting point for our future work. In particular, we will generate new code C++ code for the revised Feige-Fiat-Shamir zero-knowledge protocol. Next we will develop the handshake protocol for the new FFS. We will next develop the test databed. With the test bed we will do:

- Distributed testing
- Speed up protocol development
- Testing using UAVs as needed and where possible.
- Analysis of results

- Major testing

The purpose of this work was to revisit and revise Feige-Fiat-Shamir's original ZKP scheme in order to remove the ping-pong effect and make it faster to use. To meet this goal, after we get results in phase II, we will compare the duration of authentications in the distributed client-server model for the authentication of the Prover by the Verifier in both phase I and II. The differences we get in this comparison will demonstrate the time savings when our revised Feige-Fiat-Shamir algorithm is used.

Zero Knowledge Protocols are designed to work between two parties, the Prover and the Verifier. Through verification rounds the Prover attempts to convince the Verifier he possesses a secret. Over time the Verifier may trust the Prover has a secret and allow the Prover to communication with the Verifier. The trust the Verifier has for the Prover does not transfer to other nodes of the network. Further work, as a continuation of this project, is needed to look into how the Prover earns the trust of the entire network once accepted by the Verifier.

11. CONCLUSION

In this paper, we have produced a revised Feige-Fiat-Shamir protocol scheme in which the Verifier instead of choosing one 0-1 vector as a challenge to the *Prover* now chooses a sub-matrix whose rows are individual challenge vectors. Increasing the number of challenge vectors sent to the Prover at once speeds up the growth of the Verifier's trust of the *Prover* making the whole authentication process a lot faster and more efficient. We have also developed test programs to run the algorithm in a multi thread environment. Further we have developed the necessary protocols to run the algorithm in a client-server model which gives it a real distributed environment. As we did this we took timestamps of each run and computed time growth computation with the increasing size of the primes used. Looking at the times graph raises more and interesting questions that require extending this study. Such improvements may include finding more efficient and economical ways to move matrix D from the *Verifier* to the *Prover*. In our next attempt, we will focus on ways to move this matrix more economically. We want to investigate ways to either decompose the matrix or find some other lossless compression that will cut down on the amount of data passed.

There are several other issues that are also attracting our interest. Some of these include:

- Since ANs are P2P networks, does authentication of an entity by another network entity lead to global network authentication of that entity? If not, how do we handle subsequent authentication of that entity?
- If an entity leaves the network constellation and comes back in a very short time, does this mean a new authentication? Do we need to generate a session identification code to reduce on the number of authentication requests?

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